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REDEFINING THE EMPIRICAL ZZ CETI INSTABILITY STRIP

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ABSTRACT

We use the new ZZ Ceti stars (hydrogen-atmosphere white dwarf variables; DAVs) discovered within the Sloan Digital Sky Survey (Mukadam et al. 2004) to redefine the empirical ZZ Ceti instability strip. This is the first time since the discovery of white dwarf variables in 1968 that we have a homogeneous set of spectra acquired using the same instrument on the same telescope, and with consistent data reductions, for a statistically significant sample of ZZ Ceti stars. The homogeneity of the spectra reduces the scatter in the spectroscopic temperatures, and we find a narrow instability strip of width ~950 K, from 10,850 to 11,800 K. We question the purity of the DAV instability strip, as we find several nonvariables within. We present our best fit for the red edge and our constraint for the blue edge of the instability strip, determined using a statistical approach.

Subject headings: stars: oscillations — stars: variables: other — white dwarfs

1. INTRODUCTION

Global pulsations in white dwarf stars provide the only current systematic way to study their interiors. Hydrogen-atmosphere white dwarfs (DAs) exhibit nonradial g-mode pulsations and are known as DA variables (DAVs) or ZZ Ceti stars. Bergeron et al. (1995, 2004) and Koester & Allard (2000) find these pulsators confined to the range 11,000–12,500 K for log g ~ 8.

During the course of a 15 month search, Mukadam et al. (2004, hereafter Paper I) discovered 35 new ZZ Ceti stars within the Sloan Digital Sky Survey (SDSS). This is the first time in the history of white dwarf asteroseismology that we have a statistically significant homogeneous set of ZZ Ceti spectra, acquired entirely with the same detection system, namely, the SDSS spectrograph on the 2.5 m telescope at Apache Point Observatory. All the spectra have been reduced and analyzed consistently, using the same set of model atmospheres and fitting algorithms, including the observed photometric colors (see Kleinman et al. 2004). This homogeneity should reduce the relative scatter of the variables in the Teff–log g plane and possibly allow us to see emerging new features. The sample size of known DAVs is now almost twice as large as it was at the time of the last characterization of the instability strip by Bergeron et al. (2004). However, we do not include the previously known DAVs in our analysis with the exception of G238-53, as these pulsators do not have SDSS spectra and would only serve to reduce the homogeneity of our sample.

We list the Teff and log g values of all the variables and nonvariables we discovered within the SDSS data in Paper I, along with their internal uncertainties. Note that we do not consider WD 2350–0054 in this paper, as it may be a unique pulsator; it shows pulsation periods and pulse shapes characteristic of the hot DAV stars, while the SDSS temperature determination places it below the cool edge of the instability strip. We focus on the general trends of the majority of the DAVs, and hence a discussion of WD 2350–0054 is postponed to a future date. We do not include WD 1443–0054 either, as its temperature and log g determinations are unreliable because of a missing portion in its SDSS spectrum. We include G238-53, the only previously known ZZ Ceti star with a published SDSS spectrum.

2. EMPIRICAL INSTABILITY STRIP

We show the empirical SDSS instability strip in Figure 1, as determined by 30 new ZZ Ceti stars and G238-53. We plot histograms of the observed variables as a function of temperature and log g, as well as weighted histograms (see § 2.2) for the nonvariables (not observed to vary; NOVs). Figure 1 has two striking features: a narrow strip of width 950 K and nonvariable DA white dwarfs within the instability strip.

Pulsations are believed to be an evolutionary effect in otherwise normal white dwarfs (Robinson 1979; Fontaine et al. 1985, 2003; Bergeron et al. 2004). Nonvariables in the middle of the strip bring doubt to this semiempirical premise, even if we use the uncertainties in temperature to justify the nonvariables close to the edges.

We also note that the DAV distribution appears to be nonuniform across the strip. The features of this plot are influenced by various factors, such as biases in candidate selection, nonuniform detection efficiency in the Teff–log g plane, and uncertainties, as well as systematic effects in spectroscopic temperature and log g determinations. We address these issues and their effects on the DAV distribution in the next few subsections.

2.1. Biases in Candidate Selection

We selected SDSS DAV candidates for high-speed photometry from those spectroscopically identified DA white dwarfs that lie in the temperature range 11,000–12,500 K. These temperature fits are derived by our SDSS collaborators, using the spectral fitting technique outlined in Kleinman et al. (2004). Paper I gives a discussion of other candidate...
selection methods used in our search for ZZ Ceti stars prior to the spectral fitting technique.

Our various science goals lead to some biases in selecting DAV candidates for observation. The hot DAV (hDAV) stars exhibit extreme amplitude and frequency stability (e.g., Kepler et al. 2000; Mukadam et al. 2003). We plan to search for reflex motion caused by orbiting planets around such stable pulsators (e.g., Kepler et al. 1991; Mukadam et al. 2001; Winget et al. 2003). These stable clocks drift at their cooling rate; measuring the drift rate in the absence of orbital companions allows us to calibrate our evolutionary models. These models are useful in determining ages of the Galactic disk and halo using white dwarfs as chronometers (e.g., Winget et al. 1987; Hansen et al. 2002). Therefore, we preferentially choose to observe hDAVs in the range 11,700–12,300 K to increase the sample of known stable pulsators with both the above objectives in mind. This bias is partially compensated for, as hDAVs are harder to find (see § 2.2).

We also preferentially observe DAV candidates of extreme masses. Low-mass (log \( g \leq 7.6 \)) DAVs could well be helium-core white dwarfs; pulsating He-core white dwarfs should allow us to probe their equation of state. High-mass (log \( g \geq 8.5 \)) DAVs are potentially crystallized (Winget et al. 1997; Montgomery & Winget 1999), providing a test of the theory of crystallization in stellar plasma. Metcalfe et al. (2004) present strong evidence that the massive DAV BPM 37093 is 90% crystallized.

The distribution of chosen DAV candidates also depends on the distribution of available DAV candidates. We have an additional bias because of the SDSS criteria in choosing candidates for spectroscopy. But a histogram of the available DAV candidates is consistent with a random distribution and does not reflect any systematic effects.

The nonuniform nature of the DAV distribution does not appear to be a candidate selection effect. However, we are in the domain of small-number statistics, since we observed only four DAV candidates in the range 11,350–11,500 K. Of these, two are massive and consequently expected to be low-amplitude pulsators (see § 2.2), making detection difficult. Our data are suggestive of a bimodal DAV distribution in temperature. We hope to investigate this issue further by

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**Fig. 1.**—Distribution of new SDSS DAVs and NOVs (Mukadam et al. 2004) as a function of temperature and log \( g \). We also include G238-53 in this plot. The narrow width of the instability strip and the presence of nonvariables within form the two prominent features of this figure. We also note the paucity of DAVs in the middle of the instability strip.
observing additional DAV candidates in the range 11,350–11,500 K with our collaborators.

2.2. Nonuniform Detection Efficiency

The hDAVs show relatively few pulsation modes, with low amplitudes (~0.1%–3%) and periods around 100–300 s. The cooler DAVs (cDAVs) typically show longer periods (around 600–1000 s), larger amplitudes (up to 30%), and greater amplitude variability (Kleinman et al. 1998). Massive pulsators show low amplitudes as a result of their high gravity (log \(g\) > 8.6). These distinct trends of the pulsation periods and amplitudes with temperature and log \(g\) imply that the detection efficiency must also be a function of \(T_{\text{eff}}\) and log \(g\). The detection efficiency not only varies in the \(T_{\text{eff}}-\log g\) plane, but is also dependent on weather conditions and the magnitude of the DAV candidate. Furthermore, a ZZ Ceti star may have closely spaced modes or multiplet structure, both of which cause beating effects. Some of the nonvariables in the instability strip could well be pulsators that were in the low-amplitude phase of their beating cycle during the observing run. McGraw (1977) claimed BPM 37093 to be nonvariable, but Kanaan et al. (1992) showed that it is a low-amplitude pulsator. We use the nonvariability limits to assign the nonvariable limit in millimodulation amplitudes, but Mukadam et al. (2002) found G30-20 to be a beating variable with an amplitude of 13.8 mma.1

In order to address these issues systematically, we simulate light curves of real pulsators for different conditions and compute the resulting Fourier transform (FT) to see whether the signal is detectable above noise. We utilize the real periods and amplitudes, with randomly chosen phases (to sample the beat period), to simulate 2 hr long light curves.3 We independently shuffle the magnitudes and average seeing conditions of real data on the DAVs. This ensures a realistic distribution for both these parameters. We randomly select a magnitude and seeing value from these distributions to simulate white noise, the amplitude of which is determined using a noise table based on real data. We compute an FT of the light curve and check whether the star can be identified as a pulsator or whether the signal was swamped by noise. We repeat this procedure 100 times for each DAV for different phases, magnitudes, and seeing values. Note that our noise simulation is not completely realistic, as it does not include effects due to variable seeing, gaps in the data due to clouds, and low-frequency atmospheric noise. However, it does help us understand how the detection efficiency changes in the \(T_{\text{eff}}-\log g\) plane.

We find that we are able to rediscover almost all of the average and low-mass cDAVs in the hundred simulated attempts. The high-mass (log \(g\) ≥ 8.6) DAVs with a substantially lower amplitude are recovered with a ~70% success rate. This implies that nonvariables in Figure 1 in the region log \(g\) ≥ 8.6 have a 30% chance of being low-amplitude variables. At the hot end of the instability strip, both low pulsation amplitude and beating can cause us to miss even the average or low-mass hDAVs 35 out of 100 times.

Table 1 lists the nonvariables in the instability strip along with their temperature, log \(g\), magnitude, and number of observing runs. The number after the NOV designation indicates the best nonvariability limit in millimodulation amplitudes. Based on the simulations, we assign each nonvariable a weight based on our estimate of the probability that the observed candidate is a genuine nonvariable, and not a low-amplitude or beating pulsator. We use the nonvariability limits to assign the weights 0.98, 0.95, 0.90, 0.85, 0.80, 0.70, and 0.60, for NOV1, NOV2, NOV3, NOV4, NOV5, NOV6, and NOV7 or higher, respectively. If the NOV is massive (log \(g\) ≥ 8.6), then we additionally multiply its weight by a factor of 0.7. If the NOV is close to the blue edge of the strip, then we multiply by a factor of 0.65 to account for low-amplitude and/or beating pulsators. However, if the NOV has been observed multiple times, then it is unlikely to have been missed as a result of beating. In such a case, we multiply its weight only by a factor of 0.8 instead of 0.65, to allow for a possible low-amplitude

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1 One millimagnitude (mmag) equals 0.1086% change in intensity.
2 One millimodulation amplitude (mma) corresponds to 0.1% change in intensity.
3 We generally observe the DAV candidates for 2 hr at a time when searching for new variables.
variable. We utilize these weights in § 6 to compute best-fit red and blue edges.

2.3. Uncertainties in Temperature and log g Determinations

The true external uncertainties in the SDSS Teff determinations are likely to be larger than listed in Paper I. We expect that the external uncertainties are of the order of 300 K. However, the uncertainty that is relevant in determining the width and purity of the instability strip defined by a homogeneous ensemble is the internal uncertainty.

The low signal-to-noise ratio (S/N) of the blue end of the SDSS spectra reduces the reliability of the log g values. The H8 and H9 lines depend mostly on gravity, because neighboring atoms predominantly affect higher energy levels (Hummer & Mihalas 1970), and their density depends on log g. The external uncertainties in log g for our ensemble may be as high as 0.1, twice the estimated uncertainty for the Bergeron et al. (2004) sample. We find an average log g of ±8.10 for our sample of 31 objects, while the 36 objects in Bergeron et al. (2004) average at ±8.11. G238-53 is common to both samples; Bergeron et al. (2004) derive Teff = 11,890 K and log g = 7.91, while the SDSS determination places G238-53 at Teff = 11820 ± 50 and log g = 8.02 ± 0.02. The temperature values agree within 1 σ uncertainties. Temperature is mainly determined by the continuum and the Hα, Hβ, and Hγ lines; the low S/N at the blue end of the SDSS spectra has a reduced effect on temperature determinations. The well-calibrated continuum, extending from 3800 to 9200 Å, provides an accurate temperature determination.

The gradual change in mean mass as a function of temperature for the SDSS DA white dwarf fits is addressed in Kleinman et al. (2004), and Figure 7 of their paper shows a quantitative measure of this systematic effect. The increase in log g across the width of the instability strip is only ~0.02 and implies that our determinations of cDAV masses are negligibly higher. These systematic effects are small in the range of the ZZ Ceti instability strip and cannot produce either the narrow width or the impurity of the observed strip.

We conduct a simple Monte Carlo simulation to estimate the internal Teff uncertainties of our ensemble. Using the observed pulsation characteristics, we can separate the DAVs into two classes, hDAVs and cDAVs (see § 2.2). We show the observed distribution of the hDAVs and cDAVs in the bottom panel of Figure 2. These distributions are distinct, except for three objects. On the basis of the empirical picture, we conceive that the underlying DAV distribution may look similar to that shown in the top panel of Figure 2. We perform a Monte Carlo simulation, drawing hDAVs and cDAVs randomly from the expected DAV distribution and using Gaussian uncertainties with σ = 300 K. We show the resulting distribution in the second panel; the large uncertainties cause significant overlap between the cDAVs and hDAVs, swamping the central gap. We perform a similar simulation with σ = 200 K (third panel), and it compares well with the observed distribution, considering the small numbers of the empirical distribution. This suggests that the internal uncertainties in effective temperature for our ensemble are σ ≤ 200 K for objects, provided that we believe that the hDAVs and cDAVs each span a range of at least 300 K. Note that the internal uncertainties for a few individual objects may be as large as 250–300 K.

3. PROBING THE NONUNIFORM DAV DISTRIBUTION USING PULSATION PERIODS

The mean or dominant period of a pulsator is an indicator of its effective temperature (see § 2.2). This asteroseismological relation is not highly sensitive, but it provides a technique independent of spectroscopy to study the DAV temperature distribution. We show the distribution of the dominant periods of the SDSS DAVs in Figure 3. The top right
to determine the NOV distribution shown in the middle panel. We find that although nonvariables leak into the strip, they are found mostly at the outer edges, and their number tails off within the strip. The observed NOV distribution (bottom panel) does not show any signs of tailing off within the instability strip. Rather, it displays the same number of nonvariables at the edges as in the center of the strip. This suggests that the instability strip is impure and that all the NOVs within the instability strip did not leak in because of large $T_{\text{eff}}$ uncertainties. We carried out these simulations several times to verify these results.

We compute the likelihood that the instability strip is pure based on the following two criteria. There are two ways in which a nonvariable can disappear from the instability strip: subsequent observations show it is a (low-amplitude) variable or the internal uncertainties in $T_{\text{eff}}$ prove to be large enough to allow the possibility that it may have leaked into the strip. Table 1 lists our estimates of the probabilities that the NOVs found within the strip are genuine nonvariables. The chance that NOVs may have leaked into the strip because of large internal uncertainties $\sigma = 300$ K are 0.35 for WD 0037+0031, 0.18 for WD 0050–0023, 0.13 for WD 0303–0808, 0.04 for WD 0345–0036, 0.25 for WD 0747+2503, 0.42 for WD 0853+0005, 0.15 for WD 1031+6122, 0.38 for WD 1136–0316, 0.31 for WD 1338–0023, 0.11 for WD 1342–0159, 0.28 for WD 1345+0328, 0.13 for WD 1432+0146, 0.25 for WD 1503–0052, 0.20 for WD 1658+3638, and 0.31 for WD 1726+5331. The probability that each of the above nonvariables disappears from the instability strip is then 0.48, 0.59, 0.26, 0.23, 0.33, 0.68, 0.28, 0.62, 0.41, 0.24, 0.50, 0.30, 0.36, 0.32, and 0.59, respectively.

Three or four of the above nonvariables may have an inclination angle that reduces the observed amplitude below the detection threshold. Instead of calculating various permutations, we evaluate the likelihood of the worst-case scenario. Let four NOVs that have the least chance of disappearing from the instability strip be the ones that have an unsuitable inclination angle for observing pulsations. In that case, the chance that the instability strip is pure is 0.004%. The impurity of the instability strip suggests that parameters other than just the effective temperature and log $g$ play a crucial role in deciding the fate of a DA white dwarf, i.e., whether it will pulsate or not.

5. NARROW WIDTH OF THE ZZ CETI STRIP

Computing the width of the instability strip using the effective temperatures of the hottest and coolest pulsators gives us a value, independent of our conception of the shape of the ZZ Ceti strip. Determining whether the blue and red edges continue to be linear for very high (log $g \geq 8.5$) or very low (log $g \leq 7.7$) masses is currently not possible with either our sample or the Bergeron et al. (2004) sample. The width of the instability strip calculated from the empirical edges at different values of log $g$ involves additional uncertainties from our linear visualization of the edges.

The empirical SDSS DAV instability strip spans from the hottest objects, G238–53 and WD 0825+4119, both at $T_{\text{eff}} = 11,820 \pm 170$ K, to the coolest object, WD 1732+5905, at 10,860 \pm 100 K. This span of 960 \pm 200 K is considerably smaller than the 1500 K width in the literature (Bergeron et al. 1995; Koester & Allard 2000). The hottest pulsator in the Bergeron et al. (2004) sample is G226–29, at 12,460 K, and the coolest pulsators are G30–20 and BPM 24754, at 11,070 K.

4 We made a similar plot using the dominant periods for the 36 previously known DAVs, but did not find any evidence for a bimodal distribution. Determining the dominant period of the 36 ZZ Ceti stars in the literature proved to be difficult and quite inhomogeneous compared to our own data on the SDSS DAVs.
The extent of the instability strip for the Bergeron et al. (2004) sample is then $\sim 1400$ K.

The drift rates of the stable ZZ Ceti pulsators give us a means of measuring their cooling rates (e.g., Kepler et al. 2000; Mukadam et al. 2003). Our present evolutionary cooling rates from such pulsators suggest that given a width of 950 K, a 0.6 $M_\odot$ ZZ Ceti star may spend $10^8$ yr traversing the instability strip. This agrees with theoretical calculations by Wood (1995) and Bradley et al. (1992). The narrow width constrains our understanding of the evolution of ZZ Ceti stars.

6. EMPIRICAL BLUE AND RED EDGES

We draw blue and red edges around the DAV distribution that enclose all of the variables. This is shown in Figure 5 by the solid line for the blue edge and the dash-dotted line for the red edge. These edges also include nonvariables within the instability strip.

We now demonstrate an innovative statistical approach to find the best-fit blue and red edges that maximize the number of variables and minimize the number of nonvariables enclosed within the strip. To the best of our knowledge, no standard technique can be used to solve this interesting statistical problem. Our statistical approach has two advantages: we are accounting for the uncertainties in temperature and log $g$ values and we are utilizing most of the variables and nonvariables in our determination, rather than just a handful close to the edge.

This problem has essentially two independent sources of uncertainties: the uncertainties in temperature and log $g$ that shift the location of a star in the $T_{\text{eff}}$–log $g$ plane and the uncertainty concerning the genuine nature of a nonvariable. Pulsators masquerading as nonvariables can significantly alter our determination of the blue and red edges. Hence, we assign different weights to DAVs and NOVs. Since the DAVs are confirmed variables, we assign them a unit weight. We use the nonvariability limit to decide the weight of all the NOVs that lie outside the empirical ZZ Ceti strip, as in § 2.2, while we assign the weights listed in Table 1 for NOVs within the instability strip.

6.1. Technique

We construct a grid in $T_{\text{eff}}$ and log $g$ space in the respective ranges 9000–14,000 K and 6.0–10.5 with resolutions of 50 K.
and 0.05. For each point in the grid, we consider possible blue and red edges that vary in inclination angle relative to the temperature axis from 15° to 165° by half a degree with each successive iteration.

For each point of the grid, and for each possible blue edge, we compute a net count as follows: DAVs on the cooler side of the edge count as +1 each and on the hotter side as −1 each. NOVs on the hotter side of the edge count as +w each and on the cooler side as −w each, where w is the weight of the corresponding NOV. To determine the best blue edge, we consider all DAVs and NOVs that satisfy Teff ≥ 11,500 K. This ensures that the NOVs close to and beyond the red edge do not influence the determination of the blue edge. If the DAV or NOV is within 3σ of the edge, then we determine the net chance that it lies on the hot or cool side of the edge, assuming a Gaussian uncertainty distribution. We multiply this chance with the count for that object, before adding it to the total count. An effect of this choice is that the best edge is determined by the global distribution of DAVs and NOVs, rather than the few close to the edge.

Similarly, we determine the best red edge at each point of the grid by counting DAVs on the hotter side of the edge as +1 and NOVs on its cooler side as +w, and vice versa. We consider all DAVs and NOVs within the instability strip and cooler than 11,820 K to factor into the computation of the best red edge. If the DAV or NOV is within 3σ of the edge, then its contribution is a fraction of the above, depending on the probability that it lies on one side of the edge or the other.

To test our statistical approach, we input the Teff and log g determinations of the previously known DAVs from Bergeron et al. (2004) along with the SDSS NOVs. The resulting red and blue edges are fairly similar to those of Bergeron et al. (2004), and we attribute most of the difference to using an independent set of NOVs. Figure 5 shows our best-fit for the red edge and our constraint on the blue edge using our statistical approach. For the blue edge, we determine (1) the best-fit equation to be log g = 0.00437Teff−43.48, (2) the +1σ equation to be log g = 0.0016Teff−10.64, and (3) the −1σ equation to be log g = 0.0037Teff−36.35. For the red edge, we determine (1) the best-fit equation to be log g = 0.0010Teff−3.01 and (2) the +1σ equation to be log g = 0.0012Teff−4.73.

6.2. Estimating the Uncertainties

The dominant effect that dictates the uncertainties in the slope (log g dependence) and location (in temperature) of the edges arises as a result of the unreliable nature of the NOVs. Are they genuine NOVs or low-amplitude pulsators? Our simulations in § 2.2 show that we miss 30% of high-mass pulsators as a result of their low amplitude. We estimate that this should introduce an uncertainty of order 0.2 in the total count for both the red and blue edges. The NOVs close to the blue edge, but within the instability strip, can introduce additional uncertainties in our determination. We add these independent sources of uncertainty in quadrature to obtain an estimated 1σ uncertainty of 0.6 for the red edge and 0.4 for the blue edge. We show these as dotted lines in Figure 5. Our estimates of the 1σ uncertainties clearly show that the red edge is well constrained, and the slope of the blue edge is not.

Note that we already account for the uncertainties in Teff and log g in determining the red and blue edges. The unreliability of these uncertainties contributes toward an uncertainty in the slope of the edges; this turns out to be a negligible second-order effect.

6.3. Comparison with Empirical Edges

We show the empirical blue and red edges from Bergeron et al. (2004) in Figure 5 for comparison. The slopes of the red edges from both samples agree within the uncertainties. But our constraint on the blue edge differs significantly from that of Bergeron et al. (2004) and suggests that the dependence on mass is less severe.

The mean temperature of our sample is 11,400 K, while the mean temperature for the Bergeron et al. (2004) sample is 11,630 K. The observed extent of our instability strip defined by 31 objects spans 10,850–11,800 K, while that of Bergeron et al. (2004) spans 11,070–12,460 K. We can consider these values to imply a relative shift of ~200 K between our sample and that of Bergeron et al. (2004).

We would also like to point out that our sample is magnitude-limited and reaches out to g = 19.3. We are effectively sampling a different population of stars, more distant by a factor of 10, from the Bergeron et al. (2004) sample.

6.4. Comparison with Theoretical Edges

In Figure 5, we show the theoretical blue edge from Brassard & Fontaine (1997) due to the traditional radiative driving mechanism; they use an ML2/α = 0.6 prescription for convection in their equilibrium models. We also show the blue and red edges that we derive from the convective driving theory of Wu & Goldreich (Brickhill 1991; Wu 1998; Wu & Goldreich 1999), assuming ML2/α = 0.8 for convection.

We see that the blue edges of the two theories are essentially the same and would nearly coincide if the mixing-length parameter were tuned. To obtain the red edge of Wu & Goldreich, we have made the following assumptions: (1) the relative flux variation at the base of the convection zone is no larger than 50%, (2) the period of a representative red edge mode is 1000 s, and (3) the detection limit for intensity variations is 1 mma. Within this theory, the convection zone attenuates the flux at its base by a factor of ~ωτce, where τce is the thermal response time of the convection zone, so we have adjusted τce such that the surface amplitude 0.5/(ωτce) ~ 10^-3, equal to the detection threshold.

The observed distribution of variables and nonvariables suggests that the mass dependence of the blue edge is less severe than predicted by the models. Both the slope and the location of the red edge we calculate are consistent with the observed variables and nonvariables within the uncertainties.

7. CONCLUSION

Using a statistically significant and truly homogeneous set of 31 ZZ Ceti spectra, we find a narrow instability strip between 10,850 and 11,800 K. We also find nonvariables within the strip and compute the likelihood that the instability strip is pure to ~0.004%. Obtaining higher S/N spectra of all the SDSS and non-SDSS DAVs, as well as nonvariables, in the ZZ Ceti strip is crucial to improving our determination of the width and edges of the instability strip, and in investigating the purity of the instability strip. This should help constrain our understanding of pulsations in ZZ Ceti stars.

The DAV distribution shows a scarcity of DAVs in the range 11,350–11,500 K. After exploring various possible causes for such a bimodal, nonuniform distribution, we are still not...
entirely confident that it is real. The data at hand suggest that the nonuniformity of the DAV distribution is real and stayed hidden from us for decades as a result of the inhomogeneity of the spectra of the previously known DAVs. However, we are in the domain of small-number statistics, and unless we investigate additional targets in the middle of the strip, we cannot be confident that the bimodal distribution is not an artifact in our data.

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